



COMP 1023 Introduction to Python Programming

Python Basic Operations

Dr. James Cheung, Dr. Wilfred Ng, Dr. Desmond Tsoi

Department of Computer Science & Engineering
The Hong Kong University of Science and Technology, Hong Kong SAR, China



Introduction

- According to what we covered in the last topic, now you should know the following:
 - The **basic structure** of Python programs.
 - Python programs can “**memorize**” **data through objects referenced by variables**.
 - Using **input** and **print** functions, we can **read data from and write data** to I/O devices (e.g., keyboard, monitor, etc.).
- In this topic, we will continue to discuss more about Python programming, particularly the basic operations that Python programs can perform.
- Topics to be discussed include:
 1. **Arithmetic** operations (also known as mathematical operations).
 2. **Relational** (Comparison) operations.
 3. **Logical** operations.
 4. **Other** operations.



Part I

Arithmetic Operations



Arithmetic Operations

- In Python, the following **arithmetic operations** are supported:

Symbol(s)	Meaning	Example	Result
+	Addition	34 + 1	35
-	Subtraction	34.0 - 0.1	33.9
*	Multiplication	300 * 30	9000
/	Float division	1 / 2	0.5
//	Integer division	1 // 2	0
**	Exponentiation	4 ** 0.5	2.0
%	Remainder	20 % 3	2

- +, -, *, /, //, **, % are called **arithmetic operators**.
- The input (or arguments) around the operators are called **arithmetic operands**.

Note

To improve readability, Python allows us to **use underscores to separate digits** in a number literal. For example:

```
value = 232_45_4519
```

```
amount = 23.24_4545_4519_3415
```

However, 45_ or _45 is **incorrect**. The underscore must be placed between two digits.

What Can You Conclude From These?

Operator(s)	Example	Result
+	1 + 2	3
	1 + 2.0	3.0
	1.0 + 2	3.0
	1.0 + 2.0	3.0
-	1 - 2	-1
	1 - 2.0	-1.0
	1.0 - 2	-1.0
	1.0 - 2.0	-1.0
*	1 * 2	2
	1 * 2.0	2.0
	1.0 * 2	2.0
	1.0 * 2.0	2.0
/	1 / 2	0.5
	1 / 2.0	0.5
	1.0 / 2	0.5
	1.0 / 2.0	0.5

- In Python, if **one of the operands** for +, -, * **is of float type**, the **result** of the operation will also be **float**.

In fact, this **also applies** to //, **, and %, which we will introduce later.

- For /, the **result** will always be **float**.

Note

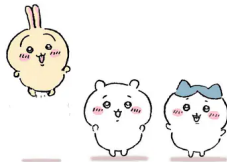
If **an integer and a float** are involved in a binary operation, Python automatically **converts the integer to a float value**. This is called **implicit type conversion**.



Arithmetic Operations

```
def main(): # Filename: arithmetic_operations.py
    # Addition
    print('1 + 2 =', 1 + 2, 'and type is', type(1 + 2))
    print('1 + 2.0 =', 1 + 2.0, 'and type is', type(1 + 2.0))
    print('1.0 + 2 =', 1.0 + 2, 'and type is', type(1.0 + 2))
    print('1.0 + 2.0 =', 1.0 + 2.0, 'and type is', type(1.0 + 2.0))
    # Subtraction
    print('1 - 2 =', 1 - 2, 'and type is', type(1 - 2))
    print('1 - 2.0 =', 1 - 2.0, 'and type is', type(1 - 2.0))
    print('1.0 - 2 =', 1.0 - 2, 'and type is', type(1.0 - 2))
    print('1.0 - 2.0 =', 1.0 - 2.0, 'and type is', type(1.0 - 2.0))
    # Multiplication
    print('1 * 2 =', 1 * 2, 'and type is', type(1 * 2))
    print('1 * 2.0 =', 1 * 2.0, 'and type is', type(1 * 2.0))
    print('1.0 * 2 =', 1.0 * 2, 'and type is', type(1.0 * 2))
    print('1.0 * 2.0 =', 1.0 * 2.0, 'and type is', type(1.0 * 2.0))
    # Division
    print('1 / 2 =', 1 / 2, 'and type is', type(1 / 2))
    print('1 / 2.0 =', 1 / 2.0, 'and type is', type(1 / 2.0))
    print('1.0 / 2 =', 1.0 / 2, 'and type is', type(1.0 / 2))
    print('1.0 / 2.0 =', 1.0 / 2.0, 'and type is', type(1.0 / 2.0))

if __name__ == "__main__":
    main()
```



Output of Arithmetic Operations

$1 + 2 = 3$ and type is `<class 'int'>`
 $1 + 2.0 = 3.0$ and type is `<class 'float'>`
 $1.0 + 2 = 3.0$ and type is `<class 'float'>`
 $1.0 + 2.0 = 3.0$ and type is `<class 'float'>`

$1 - 2 = -1$ and type is `<class 'int'>`
 $1 - 2.0 = -1.0$ and type is `<class 'float'>`
 $1.0 - 2 = -1.0$ and type is `<class 'float'>`
 $1.0 - 2.0 = -1.0$ and type is `<class 'float'>`

$1 * 2 = 2$ and type is `<class 'int'>`
 $1 * 2.0 = 2.0$ and type is `<class 'float'>`
 $1.0 * 2 = 2.0$ and type is `<class 'float'>`
 $1.0 * 2.0 = 2.0$ and type is `<class 'float'>`

$1 / 2 = 0.5$ and type is `<class 'float'>`
 $1 / 2.0 = 0.5$ and type is `<class 'float'>`
 $1.0 / 2 = 0.5$ and type is `<class 'float'>`
 $1.0 / 2.0 = 0.5$ and type is `<class 'float'>`

Can you solve this ?

Hmmm ... I can't



So, I erase it ...



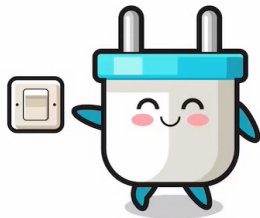
Integer Division (//)

- The operator `//` is used for **integer division**, also known as **floor division**.
- The `//` operator divides two numbers and returns the **largest integer that is less than or equal to the result** (the floor of the division).
- Examples:
 - `5 // 2` returns 2, because 5 divided by 2 is 2.5, and the largest integer less than or equal to 2.5 is 2.
 - `5.0 // 2` returns 2.0, because the result is a float.
 - `5 // 2.0` also returns 2.0.
 - `5.5 // 2` returns 2.0, as the largest integer less than or equal to 2.75 is 2.
 - `5.5 // -2` returns -3.0, as the largest integer less than or equal to -2.75 is -3.



Exponentiation (**)

- The operator `**` is used for **exponentiation**, which **raises a number (the base) to the power of another number (the exponent)**.
- Examples:
 - `2 ** 3` evaluates to 8, because it is equivalent to $2^3 = 8$.
 - `4.0 ** 0.5` evaluates to 2.0, because it is equivalent to $4.0^{0.5} = 4.0^{\frac{1}{2}} = \sqrt{4.0} = 2.0$.
 - `2 ** -2` evaluates to 0.25, because it is equivalent to $2^{-2} = \frac{1}{2^2} = 0.25$.
 - `2 ** 3 ** 2` evaluates to 512, because it is equivalent to $2^{(3**2)}$, which is 2^9 and equals 512.
 - **Tricky:** `(-1) ** 0.5` evaluates to `1j`, because it is equivalent to $\sqrt{-1}$, and equal to $6.123233995736766e-17 + 1j$.



Modulo Operation (%)

- The arithmetic operator % is referred to as the “modulo operator”, “mod operator”, or simply “mod”.
- It is used to find the remainder after integer division.

$$\begin{array}{r} 2 \\ 3 \overline{) 7} \\ \underline{6} \\ 1 \end{array} \quad \begin{array}{r} 0 \\ 7 \overline{) 3} \\ \underline{0} \\ 3 \end{array} \quad \begin{array}{r} 3 \\ 4 \overline{) 12} \\ \underline{12} \\ 0 \end{array} \quad \begin{array}{r} 3 \\ 8 \overline{) 26} \\ \underline{24} \\ 2 \end{array} \quad \text{Divisor} \longrightarrow \begin{array}{r} 1 \\ 13 \overline{) 20} \\ \underline{13} \\ 7 \end{array} \begin{array}{l} \longleftarrow \text{Quotient} \\ \longleftarrow \text{Dividend} \\ \longleftarrow \text{Remainder} \end{array}$$

- The modulo operator has many useful applications in computer programs:
 - Testing whether a number is even or odd: `number % 2 == 0` for even numbers, `number % 2 == 1` for odd numbers.
 - Finding individual digits of a number: `number % 10` gives the least significant digit (rightmost digit) of the number.
 - Finding the last four digits of an HKID number: `ID % 10000`.

Modulo Operations

```
# Filename: mod_operations.py
# An example demonstrating mod operations
def main():
    print('1023 % 2 is', 1023 % 2)           # Remainder when 1023 is divided by 2
    print('1023 % 10 is', 1023 % 10)        # Remainder when 1023 is divided by 10
    print('1023 % 100 is', 1023 % 100)      # Remainder when 1023 is divided by 100
    print('1023 % 1000 is', 1023 % 1000)    # Remainder when 1023 is divided by 1000
    # Last 4 digits of ID
    print('The last 4 digits of ID: 8121232 % 10000 is', 8121232 % 10000)

if __name__ == "__main__":
    main()
```

Output:

```
The result of 1023 % 2 is 1
The result of 1023 % 10 is 3
The result of 1023 % 100 is 23
The result of 1023 % 1000 is 23
The last 4 digits of ID: 8121232 % 10000 is 1232
```

Display Time

- This program converts an amount of time given in seconds into minutes and remaining seconds.

```
# Filename: display_time.py  
# A program that obtains minutes and remaining seconds from an amount of time in seconds  
def main():  
    # Prompt the user for input  
    seconds = int(input("Enter an integer for seconds: "))  
  
    # Calculate minutes and remaining seconds  
    minutes = seconds // 60 # Calculate whole minutes  
    remaining_seconds = seconds % 60 # Calculate remaining seconds  
  
    # Display the result  
    print(seconds, "seconds is", minutes, "minutes and", remaining_seconds, "seconds")  
  
if __name__ == "__main__":  
    main()
```

Output:



More about Modulo Operations

- The operands of the modulo operator can be positive or negative integers or floats.
- For $a \% b$, it is computed based on the following formula:

$$r = a - (a // b) * b$$

- Examples:

- $10 \% 3 = 10 - (10 // 3) * 3 = 10 - 3 * 3 = 1$
- $10 \% -3 = 10 - (10 // -3) * (-3) = 10 - (-4) * (-3) = 10 - 12 = -2$
- $-10 \% 3 = -10 - (-10 // 3) * 3 = -10 - (-4) * 3 = -10 + 12 = 2$
- $-10 \% -3 = -10 - (-10 // -3) * (-3) = -10 - 3 * (-3) = -10 + 9 = -1$
- $-5.3 \% 3 = -5.3 - (-5.3 // 3) * 3 = -5.3 - (-2) * 3 = -5.3 + 6 = 0.7$
- $5.3 \% -3 = 5.3 - (5.3 // -3) * (-3) = 5.3 - (-2) * (-3) = 5.3 - 6 = -0.7$
- $-5.3 \% -3 = -5.3 - (-5.3 // -3) * (-3) = -5.3 - 1 * (-3) = -5.3 + 3 = -2.3$

Can you calculate $6.4 \% -1.7$?

Subtraction and Negation Operations (-)

- The operator `-` is used as both a **binary subtraction** operator and a **unary negation** operator.
 - The **binary subtraction** operator takes **2 operands** (e.g., `10 - 20`).
 - The **unary negation** operator takes **1 operand** (e.g., `-3`).

```
# Filename: subtraction_negation.py
```

```
def main():  
    print("The result of 10 - 20 is", 10 - 20) # Subtraction  
    print("This is", -3)                       # Negation  
  
if __name__ == "__main__":  
    main()
```

Output:

```
The result of 10 - 20 is -10  
This is -3
```



Division by Zero in Python

- Division by zero is an **error** in Python.
- Common operations that raise this error:

- Division:

```
result = 5 / 0    # Raises ZeroDivisionError
```

- Integer Division:

```
result = 5 // 0   # Raises ZeroDivisionError
```

- Modulo:

```
result = 5 % 0    # Raises ZeroDivisionError
```

- Exponentiation:

```
result = 0 ** 0   # This is defined as 1
```



Always check for zero before performing division or related operations!

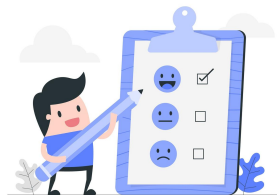
Expressions

- In programming, we often need to include values and operations; the technical term for these is expressions.
- An **expression** is a **simple value or a combination of operations that produces a value**.
- Examples:
 - Simplest expressions (just an integer or a floating-point literal): 89 or 30.23.
 - A combination of operations that produces a value:

$$(3 * 7) + (4 * 4) + 8$$

(The resulting value of the above expression is 45).

The **process** of obtaining the value of an expression is called **evaluation**.

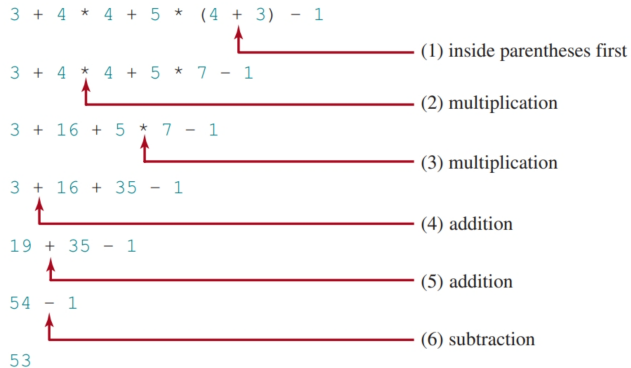


Precedence of Arithmetic Operators

Q: If there are multiple operators involved in an expression, how should we evaluate it?

- This is determined by the **precedence of operators**.
- **Operator precedence determines the order in which operations are performed in an expression.**
- For arithmetic expressions, there are three levels of precedence:
 - **Exponentiation** ($**$) is applied first.
 - **Multiplication** ($*$), **float division** ($/$), **integer division** ($//$), and **remainder** ($\%$) operators are applied next. If an expression contains several of these operations, they are applied from **left to right**.
 - **Addition** ($+$) and **subtraction** ($-$) operators are applied last. If an expression contains multiple addition and subtraction operators, they are also applied from left to right.
- Can I override these rules?
Yes, by using **parentheses** ($()$).

Precedence of Arithmetic Operators



- This diagram illustrates the **precedence of arithmetic operators** in Python.
- Higher precedence operators are evaluated before lower precedence operators.
- Use parentheses to override the default precedence rules.

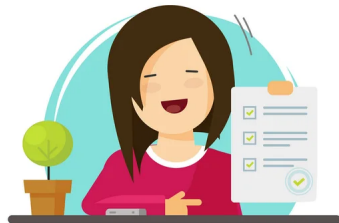
Precedence of Arithmetic Operators

Filename: precedence_arithmetic_operators.py

```
def main():  
    print("The result of 3 + 4 * 4 + 5 * (4 + 3) - 1 is",  
          3 + 4 * 4 + 5 * (4 + 3) - 1)  
  
if __name__ == "__main__":  
    main()
```

Output:

The result of 3 + 4 * 4 + 5 * (4 + 3) - 1 is 53



Arithmetic Operations on Variables

- Arithmetic operators can also be applied to variables.
- The precedence of operations remains the same when using variables.
- This example demonstrates various arithmetic operations on variables:

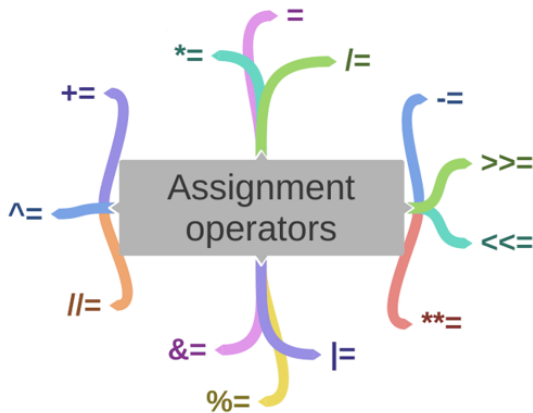
```
def main():  
    a, c = 10, 22  
    b, d = 20.1, 18.9  
    print("Addition:", a + b)  
    print("Subtraction:", a - b)  
    print("Multiplication:", a * b)  
    print("Division:", a / b)  
    # The following has a precision error  
    print("Combination:", a * 10 + b / c - d + 6)  
  
if __name__ == "__main__":  
    main()
```

Output:

```
Addition: 30.1  
Subtraction: -10.100000000000001  
Multiplication: 201.0  
Division: 0.49751243781094523  
Combination: 88.01363636363635
```

Part II

Assignment Operation



Assignment Operation

- The **assignment operator** = is used to **assign a value to an object referenced by a variable**.

Syntax

```
<var name> = <initial value>
```

```
# Cascading assignment
```

```
<var name1> = <var name2> = <initial value>
```

```
# Simultaneous assignments
```

```
<var name1>, <var name2>, ... = <initial value1>, <initial value2>, ...
```

```
<var name> = <expression>
```

```
<var name1> = <var name2> = <expression>
```

```
<var name1>, <var name2>, ... = <expression1>, <expression2>, ...
```

where <var name> or <var nameN> is the variable name in the program, referring to its location in memory; <initial value> or <initial valueN> is the value initially assigned to the object referenced by a variable (this is called **initialization**); <expression> or <expressionN> refers to a value obtained from operations.

Assignment Operation

- Examples:

Simultaneous assignments

$x, y = 3, 4$ *# Create objects with values 3 and 4 and referenced by x and y*

$x = 2 + 9$ *# Create an object with the result of $2 + 9$ (11) and referenced by x*

$x = y$ *# Create an object to store the value of y (4) and referenced by x*

$x = x + 1$ *# Create an object to store the value of $x + 1$ (5) and referenced by x*

- Common Confusion:

- Many students may get confused because **assignment statements**, such as $x = x + 1$, **do not follow traditional mathematical rules**.

- In mathematics, no real number can satisfy the equation $x = x + 1$.

However, in programming, we are **simply assigning the value of $(x + 1)$ to the variable x** . This is not a mathematical equation, but an assignment operation.



Assignment Operation

Filename: bmi_example.py

```
def main():  
    weight, height = 195, 70 # Initialize weight and height  
    bmi = weight / (height * height) * 703 # Calculate BMI  
    print("Previous BMI:", bmi)  
  
    weight = 180 # Update weight  
    bmi = weight / (height * height) * 703 # Recalculate BMI  
    print("Current BMI:", bmi)  
  
if __name__ == "__main__":  
    main()
```

Output:

Previous BMI: 27.976530612244897

Current BMI: 25.82448979591837



What is Wrong in This Code?

```
def main():  
    count = count + 1  # Error: count is not defined yet  
    print(count)  
  
if __name__ == "__main__":  
    main()
```

- An **error occurs** in the line `count = count + 1` because the **variable count has not been defined** before this line.
- To fix it, we can **define the object referenced by the variable count** first:

```
def main():  
    count = 1          # Initialize count  
    count = count + 1  # Increment count by 1  
    print(count)  
  
if __name__ == "__main__":  
    main()
```

Simultaneous Assignments and Cascading Assignments

Filename: simultaneous_cascading_assignment.py

```
def main():  
    x, y = 10, 20  # Simultaneous assignments  
    ''' This is equivalent to:  
        x = 10  
        y = 20 '''  
    print(x, y)  
  
    i = j = k = 1  # Cascading assignments  
    ''' This is equivalent to:  
        temp = 1  
        i = 1  
        j = 1  
        k = 1 '''  
    print(i, j, k)  
  
if __name__ == "__main__":  
    main()
```

Output:

10 20
1 1 1



Assignment Operation - Swapping Two Variables

```
# Filename: swapping.py
def main():
    x = 5
    y = 10

    # Swap x with y
    x, y = y, x
    print(f"x: {x}, y: {y}")

    ''' x, y = y, x
    is equivalent to:
        temp = x
        x = y
        y = temp '''

if __name__ == "__main__":
    main()
```

How it Works?

We will discuss this in detail when we talk about tuples!

- **Tuple Packing:** On the right side of the assignment (y, x), Python **creates a tuple** containing the current values of y and x. For example, if x is 5 and y is 10, the expression (y, x) evaluates to the tuple (10, 5).
- **Tuple Unpacking:** On the left side of the assignment, the values from this tuple are **unpacked into the variables** x and y. In this case, x will get the value of 10, and y will get the value of 5.

Augmented Assignment Operations

- Python allows **augmented assignment operations** to simplify coding.

Operator	Description	Example	Equivalent
<code>+=</code>	Addition assignment	<code>i += 8</code>	<code>i = i + 8</code>
<code>-=</code>	Subtraction assignment	<code>i -= 8</code>	<code>i = i - 8</code>
<code>*=</code>	Multiplication assignment	<code>i *= 8</code>	<code>i = i * 8</code>
<code>/=</code>	Float division assignment	<code>i /= 8</code>	<code>i = i / 8</code>
<code>//=</code>	Integer division assignment	<code>i //= 8</code>	<code>i = i // 8</code>
<code>%=</code>	Remainder assignment	<code>i %= 8</code>	<code>i = i % 8</code>
<code>**=</code>	Exponentiation assignment	<code>i **= 8</code>	<code>i = i ** 8</code>

These augmented assignment operators are **syntactic sugar**, providing more **convenient and expressive ways to perform operations** that could be done with more verbose syntax.

- Example:
 - `x /= 4 + 5.5 + 1.5` is equivalent to `x = x / (4 + 5.5 + 1.5)`.

Note

There are **no spaces** in augmented assignment operators. For example, `+=` should not have a space.

Augmented Assignment Operation

Filename: augmented_assignment.py

```
def main():  
    account = 2000.0  
    income = 1000.0  
    print("Account =", account, ", income =", income)  
    account += income # Augmented assignment to update account  
    print("Account =", account, ", income =", income)  
  
if __name__ == "__main__":  
    main()
```

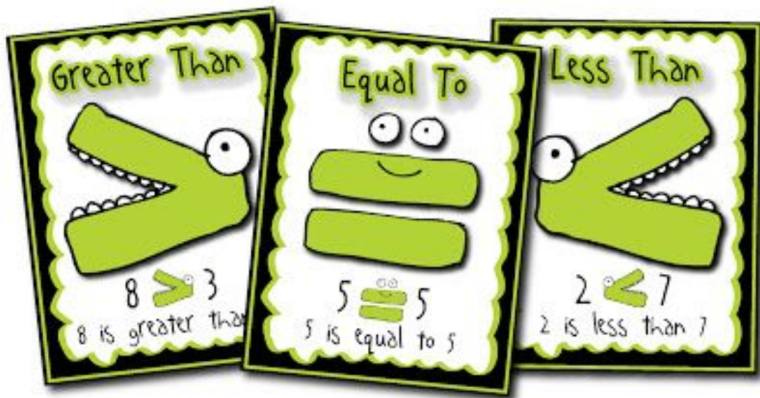
Output:

```
Account = 2000.0 , income = 1000.0  
Account = 3000.0 , income = 1000.0
```



Part III

Relational (Comparison) Operations



Relational Operations

- Relational (comparison) operators define the **relationships** between values.

Operator	Maths Symbol	Description	Example (radius is 5)	Result
<	<	less than	radius < 0	False
<=	≤	less than or equal to	radius <= 0	False
>	>	greater than	radius > 0	True
>=	≥	greater than or equal to	radius >= 0	True
==	=	equal to	radius == 0	False
!=	≠	not equal to	radius != 0	True

- The **result** of the comparison is a **Boolean value**: **True** or **False**.

```
radius = 5
```

```
print(radius > 0)  # Prints True
```



Relational Operations

```
def main(): # Filename: relational_operations.py
    x = 10
    y = 20
    x_greater_than_y = (x > y)
    x_greater_than_equal_y = (x >= y)
    x_less_than_y = (x < y)
    x_less_than_equal_y = (x <= y)
    x_equal_y = (x == y)
    x_not_equal_y = (x != y)

    print("x, y:", x, y)
    print("x > y:", x_greater_than_y)
    print("x >= y:", x_greater_than_equal_y)
    print("x < y:", x_less_than_y)
    print("x <= y:", x_less_than_equal_y)
    print("x == y:", x_equal_y)
    print("x != y:", x_not_equal_y)

if __name__ == "__main__":
    main()
```

Output:

```
x, y: 10 20
x > y: False
x >= y: False
x < y: True
x <= y: True
x == y: False
x != y: True
```



String Comparisons in Python

- Strings in Python can be compared using relational operators: `<`, `>`, `<=`, `>=`, `==`, `!=`
- Comparisons are based on **lexicographical order**, which is **determined by the ASCII values of characters**.

ASCII Code Explanation

- Each character has a corresponding ASCII value:
 - `'a'` = 97, `'b'` = 98, `'c'` = 99
 - `'A'` = 65, `'B'` = 66
- When comparing strings:
 - Compare the ASCII values of each character from left to right.
 - The string with the smaller ASCII value comes first.
- Examples:
 - `"apple" < "banana": 'a' (97) < 'b' (98) (True)`
 - `"Box" < "Boy": 'x' (120) < 'y' (121) (True)`

Part IV

Logical Operations



Logical Operations

- There are three **logical operators** in Python:

Operator	Description
not	logical negation
and	logical conjunction
or	logical disjunction

- Logical operators combine two Boolean values and produce a single Boolean result** based on the corresponding **truth table**.

Truth Table				
p	q	p and q	p or q	not p
True	True	True	True	False
True	False	False	True	False
False	True	False	True	True
False	False	False	False	True

- The variables **p** and **q** can be **Boolean literal values** or **evaluated Boolean values from expressions**.

Logical Operations

- Return True if x is in the range $[3, 10]$:

```
in_range = ( (x >= 3) and (x <= 10) )
```

Python supports chained comparison operators:

```
# in_range = ( 3 <= x <= 10 ) # Equivalent statement
```

- Return True if $|x| > 1$:

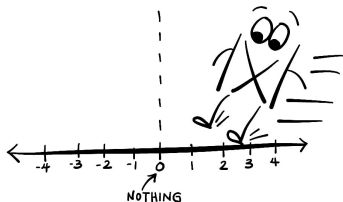
- $\text{abs_x_greater_than_1} = ((x > 1) \text{ or } (x < -1))$

- Return True if x is not equal to 0. The two statements below are equivalent:

- $\text{non_zero} = (x \neq 0)$

- $\text{non_zero} = \text{not}(x == 0)$

ABSOLUTE VALUE WILL STOP AT
NOTHING TO STAY POSITIVE!



Example: Determining Leap Years

- A leap year has 366 days. The February of a leap year has 29 days.
- A leap year is divisible by 4 but not by 100, or divisible by 400

```
def main(): # Filename: leap_year.py
    year = int(input("Enter a year: "))

    # Check if the year is a leap year
    is_leap_year = (year % 4 == 0 and year % 100 != 0) or \
        (year % 400 == 0)

    # Display the result
    print(year, "is a leap year?", is_leap_year)

if __name__ == "__main__":
    main()
```

Output:



Short Circuiting or Lazy Operations

- **Short-circuiting** is a technique where the execution of a boolean expression containing 'or' and 'and' operators is halted as soon as the truth value of the expression is determined.
- This technique makes computation faster by not evaluating the remaining expressions once the truth value is established.

Operation	Notes
p or q	q is executed only if p is False
p and q	q is executed only if p is True

- The evaluation of expressions takes place from left to right.

```
print(True or 2/0)    # Evaluates to True, 2/0 is not evaluated
print(False or 2/0)   # This raises an error, since 2/0 is evaluated
```

```
print(False and 2/0)  # Evaluates to False, 2/0 is not evaluated
print(True and 2/0)   # This raises an error, since 2/0 is evaluated
```

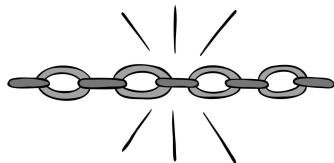
Chain Operators in Python

- Chain operators allow you to combine multiple comparisons in a single expression.
- They evaluate to 'True' if all comparisons are 'True'.
- Example:

$$5 > x > 3$$

This checks if x is greater than 3 and less than 5.

The expression $5 > x > 3$ is almost equivalent to $5 > x$ and $x > 3$.



Part V

Other Operations



Identity Operations

- **Identity operators** check if **two variables refer to the same object** in memory.
- There are two identity operators:
 - **is**: Returns **True** if both operands refer to the same object.
 - **is not**: Returns **True** if both operands do not refer to the same object.
- Use identity operators when you need to check if two variables point to the same object, not just if they are equal in value.

```
a = 1
b = 1
print(a is b)          # Print True
print(a is not b)      # Print False
```

Since both `a` and `b` are assigned the value 1, and Python caches small integers (typically between -5 and 256), both `a` and `b` refer to the same integer object in memory. Therefore, `print(a is b)` evaluates to **True**, and `print(a is not b)` evaluates to **False**.

Python Caches Small Integers

- Python **cached small integers for efficiency**, typically in the range of **-5 to 256**. But the range of these cached integers **can vary depending on the platform** and the Python implementation.
- This means that when you create an integer within this range, Python reuses the same object instead of creating a new one.

```
x = 100; y = 100  
print(x is y)  # Print True
```

- The `is` operator confirms that both `x` and `y` point to the same object in memory.
- This caching mechanism can lead to performance improvements and reduced memory usage.
- However, integers outside this range are not cached:

```
a = 1000; b = 1000  
print(a is b)  # Print True in VS Code, but False in Colab
```

- In Colab, `a` and `b` are different objects in memory.

Caching small integers is an optimization technique employed by Python to enhance performance for frequently used values.

Membership Operations

- **Membership operators** check if **an item exists within a collection**. They return a boolean value **True** or **False**.
- There are two membership operators:
 - **in**: Returns **True** if the specified item exists in a sequence; **False** otherwise.
 - **not in**: Returns **True** if the specified item does not exist in a sequence; **False** otherwise.

Note

More details will be provided when discussing collections!



Associativity of Operators

- **Associativity** refers to the **order in which operators of the same precedence are evaluated** in an expression.
- In Python, operators can be **left-to-right associative** or **right-to-left associative**.
- **Left-to-right Associative Operators:**
 - Most arithmetic operators (e.g., $+$, $-$, $*$, $/$) are left-to-right associative.
 $10 / 5 * 2$ is evaluated as $(10 / 5) * 2 = 4.0$
- **Right-to-left Associative Operators:**
 - The exponentiation operator ($**$) is right-to-left associative.
 $2 ** 3 ** 2$ is evaluated as $2 ** (3 ** 2) = 2 ** 9 = 512$



Operator Precedence from High (Top) to Low (Down)

Operator	Description	Associativity
**	Exponentiation	Right-to-left
+, -	Unary plus and minus	Right-to-left
*, /, //, %	Multiplication, division, integer division, and modulus	Left-to-right
+, -	Binary addition and subtraction	Left-to-right
<, <=, >, >=	Relational operators	Left-to-right
==, !=	Equality operators	Left-to-right
is, is not	Identity operators	Left-to-right
in, not in	Membership operators	Left-to-right
not	Logical negation	Left-to-right
and	Logical conjunction	Left-to-right
or	Logical disjunction	Left-to-right
=, +=, -=, *=, /=, //=, %=, **=	Assignment and augmented assignment operators	Right-to-left*

* Refer to the last page for more details.

Reference: <https://docs.python.org/3/reference/expressions.html>

Do not rely solely on precedence rules when writing your program.

- Be cautious: logical **and** is evaluated before logical **or**.
- Example: `(p or q and r)` is equivalent to `(p or (q and r))`. Use parentheses to clarify your intention.

Floating Point Errors in Python

- Occur due to the way floating point numbers are represented in computer memory.
- Can lead to precision loss and unexpected results in calculations.
- Common Causes:
 - Precision Limitations:
 - Floating point numbers have limited precision (typically 15-17 decimal digits).
 - Example: `0.1 + 0.2` may not equal `0.3`.
 - Rounding Errors:
 - Operations can introduce small errors due to rounding.
 - Example: `print(0.1 + 0.2 == 0.3)` results in `False`.
- Handling Floating Point Errors:
 - Use the `math.isclose()` function for comparisons:

```
import math
print(math.isclose(0.1 + 0.2, 0.3))  # Print True
```
 - Consider using the `decimal` module for higher precision:

```
from decimal import Decimal
print(Decimal('0.1') + Decimal('0.2') == Decimal('0.3'))  # Print True
```

Common Pitfalls in Python Programming

- **Confusion** between **Assignment** and **Equality**:
 - The assignment operator `=` is used to assign values to variables.
 - The equality operator `==` is used to compare two values.
 - Common mistake: Using `=` when you meant to use `==`.
- **Misunderstanding Operator Precedence**:
 - Operators have different levels of precedence, which affects the order of operations.
 - Example: In the expression `a + b * c`, multiplication is performed before addition.
 - Common mistake: Assuming operations will be executed from left to right without considering precedence.
- Using **`is`** vs. `==`:
 - The **`is`** operator checks for identity (same object in memory), while `==` checks for equality (same value).
 - Common Mistake: Using **`is`** to compare values instead of `==`. An exception is to use **`is`** when comparing with **`None`**.

Key Terms

- Arithmetic operators/operations
- Assignment operator/operations
- Augmented assignment operators/operations
- Cascading assignments
- Evaluations
- Expressions
- Exponentiation
- Identity operators/operations
- Integer division
- Lazy operator
- Logical operators
- Membership operators/operations
- Modulo operation
- Negation operator/operation
- Operands
- Operators
- Precedence
- Relational operators/operations
- Short-circuit evaluation
- Simultaneous assignments
- Syntactic sugar
- Truth table

Review Questions

Fill in the blanks in each of the following sentences about the Python environment.

1. In Python, three main types of operations are _____, _____, and _____.
2. `+`, `-`, `*`, `/`, `//`, `**`, `%` are called _____, and the arguments around them are called _____.
3. When evaluating an expression with values of an `int` type and a `float` type, Python automatically converts the _____ type value to a _____ type value.
4. `//` is used for _____.
5. `**` is used for _____.
6. `%` is called the _____ operator, and is used to find the _____ after integer division.

Answer: 1. arithmetic, relational, logical, 2. operators, operands, 3. `int`, `float`, 4. integer division, 5. exponentiation, 6. modulo, remainder.

Review Questions

Fill in the blanks in each of the following sentences about the Python environment.

7. _____ is used as both a binary operator and a unary operator.
8. An _____ is a simple value or a combination of operations that produces a value.
9. _____ can be used to force the order of evaluation to occur in any sequence.
10. The _____ is used to assign a value to an object referenced by a variable.
11. The operators in arithmetic expressions are evaluated in the order determined by the rules of _____ and _____.
12. Python provides _____ operators: +=, -=, *=, /=, //=, and %=.
13. The _____ operators (<, <=, ==, !=, >, >=) yield a Boolean value.
14. Python uses _____ to represent **True**, and _____ for **False**.

Answer: 7. Operator -, 8. expression, 9. Parenthesis, 10. assignment operator, 11. parenthesis, operator precedence, 12. augmented assignment, 13. relational (or comparison), 14. (1), (0).

Review Questions

Fill in the blanks in each of the following sentences about the Python environment.

15. _____ values are considered **True** in a Boolean context, while _____ values are evaluated as **False**.
16. The logical operators _____, _____, and _____ operate with Boolean values and variables.
17. _____ is a technique where the execution of a boolean expression containing **or** and **and** operators is halted.
18. Logical _____ is evaluated before logical _____.
19. _____ operators check if two variables refer to the same object in the memory.
20. _____ operators check if an item exists, or does not exist within a sequence.

Answer: 15. Non-zero, zero, 16. **and**, **or**, **not**, 17. Short circuiting, 18. **and**, **or**, 19. Identity, 20. Membership

Further Reading

- Read Sections 2.5 - 2.6, 2.8 - 2.12, 3.2, 3.10, and 3.15 of “Introduction to Python Programming and Data Structures” textbook.



That's all!

Any questions?



Understanding Assignment Operator Associativity in Python

- In Python, the assignment operator has right associativity and follows a specific rule when there are multiple targets in a cascaded assignment statement. For example:

```
x = y = 1
```

is executed as

```
temp = 1
```

```
x = temp
```

```
y = temp
```

- This implementation strategy is specific to Python and does not apply to other programming languages like C++. Therefore, we do not plan to test students on the associativity of assignment operators in the course. Students who are interested can reach out to the instructors privately for more information.